

(8)

Code No. : B-240(A)

From a point on the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  perpendiculars are drawn on the axes and join the feet of the perpendiculars. Show that the straight lines so drawn always touches the curve

OR

Find the maximum value of  $\sin A + \sin B + \sin C$  in a triangle ABC. Use Lagrange's method.

5. Evaluate the integral  $\int_R \frac{1}{\sqrt{x^2+y^2}} dx dy$  where R is the region bounded by the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ .

OR

Change the order of integration and evaluate the following integral :

-----x-----

Roll No.....

Total No. of Section : 03

Total No. of Printed Pages : 08

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Annual Examination - 2017

B.Sc.-II

MATHEMATICS

Paper - I

ADVANCED CALCULUS

Max.Marks : 50

Min Marks : 17

Time : 3 Hrs.

Note : Section 'A' is objective type, containing 10 questions, is compulsory. Section 'B' consists of short answer type questions and Section 'C' consists of long answer type questions. Section 'A' has to be solved first.

Section 'A' (Section-'A')  
 Answer the following questions. (1x10=10)

1. Fill in the blanks) B

$$\lim_{n \rightarrow \infty} \left( \frac{1}{3} + \frac{1}{3^2} + \dots + \frac{1}{3^n} \right) = \dots\dots\dots$$

2. y n a n s y i q j a i :

$$\sum_{n=1}^{\infty} \frac{n^{n^2}}{(1+n)^{n^2}} \text{ i a s y a / i q y a n e n}$$

Choose the correct option B

The series  $\sum \frac{n^{n^2}}{(1+n)^{n^2}}$  is convergent/divergent.

P.T.O.

Zalāā-3. Äyvä f(x) = x - |x| ∀ x ∈ IR Şy ävŞ f(0-0) = ? , f(0+0) = ?

For the function

f(0-0) = ? , f(0+0) = ?

Zalāā-4. Äyvä

x = 0 ; wŞyväāu Nè uā

Function

is differentiable at x = 0 if

Zalāā-5.

Şyā ; OmŞw Nè / ; OmŞw ÄāNā Nèñ

lim (x, y) -> (0, 0) 2y/x exists/doesnot exists.

Zalāā-6. uā f\_x(a, b) = lim\_{h->0} (f(a+h, b) - f(a, b))/h ; ä

f\_y(a, b) = lim\_{k->0} (f(a, b+k) - f(a, b))/k ; f\_yy(a, b) = ?

If and

f\_y(a, b) = lim\_{k->0} (f(a, b+k) - f(a, b))/k then f\_yy(a, b) = ?.

OR

äy ÷ ŞylākŞ äŞy (Prove that) :

kNāθ, -1 ; ä Şy rāj ŞyāŞyPua Nèñ

where is a number between -1 and 1.

Zalāā-3. uā kNā r^2 = x^2 + y^2 māÄāŞyŞ

If where r^2 = x^2 + y^2 then show that :

OR

Handwritten mathematical derivation for the identity u^3 + v^3 + w^3 - 3uvw = (u+v+w)(u^2 + v^2 + w^2 - uv - vw - wu)

māŞy ÷ ŞylākŞ (Then prove that) :

Zalāā-4. Äāi uāñ

Şy äŞyā äÄāŞy ; ÖāŞy vÈr »ŞvçkāmŞy ; ä ÇÄvÈrŞ

Şy qāŞyŞyçat vāu kāmā Nèñ äy ÷ ŞylākŞ äŞy Çy ZaŞy ZaŞm ŞyÉv ÈñŞyNtŞā

wŞy

ŞyçDqİäŞyŞmā Nèñ



Zalā-2. i) ÉavçZatçı ¥wbi) 1pÉ Zatçı Şya ŞynĀ Āāā¥ ĩ

Give the statement of i) Rolle's theorem and ii) Taylor's theorem.

OR

ĀĀāuçāşy āĀāvāĥm ĀyvĀ Şy āv¥ f'(0) Şya ĩ OmĀv ĀĀā Āēß

Show that f'(0) does not exists for the following function :

$$f(x) = \begin{cases} x & x \neq 0 \\ 0 & x = 0 \end{cases}$$

Zalā-3. tāĀā f : R³ → R āĀāā Zāşyē yçqāşākm Āēāā lim (x, y) → (0,0) f(x, y)

Öāā Şylā¥ ß

Let f : R³ → R be defined as follows then find

$$\lim_{(x, y) \rightarrow (0,0)} f(x, y) :$$

$$f(x, y) = \begin{cases} xy^3 & (x, y) \neq (0,0) \\ 0 & (x, y) = (0,0) \end{cases}$$

OR

uā u = log (x⁴ + y⁴) / (x + y) māĀāuçāşy ß

If u = log (x⁴ + y⁴) / (x + y) then show that :

Zalā-4. ĩ ānqÉwvu x² - y² / a² - b² = 1 Şy Şylōk Şya ytāşyĀ Öāā Şylā¥ ĩ

Find the equation of evolute for the hyperbola .

OR

¥şy āāsk Şy ĩ ĀÉ ¥şy āĀāçy Zāşyē Öāā Şylā¥ āşy māāşyāāu āĀāā āyç Çyşyl ĀĀūāşy wāçşyā uāā āĀāāpĀēñ

Find a point inside a triangle so that the sum of squares of its distance from all three angular points is minimum.

Zalā-5. āĀāvāĥm Şya tāĀā Öāā Şylā¥ ß

Evaluate :

OR

tāuāşyā Şylā¥ ß

Evaluate :